

The Higgs Boson: Theoretical Issues

Sally Dawson

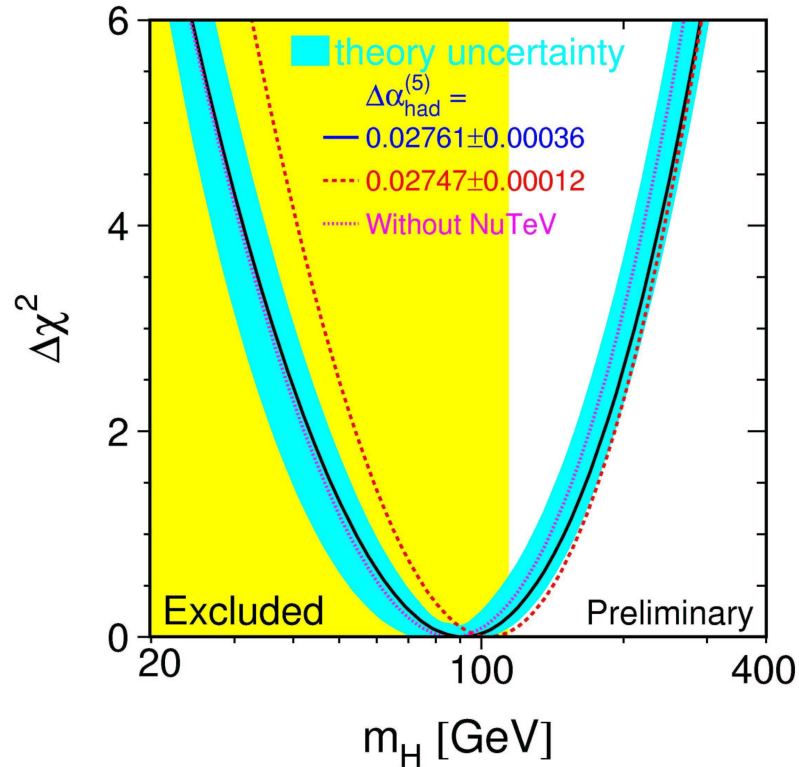
Aspen Winter Conference

February, 2004

➤ Thanks to my collaborators:

C. Jackson, L. Orr, L. Reina, D. Wackerroth

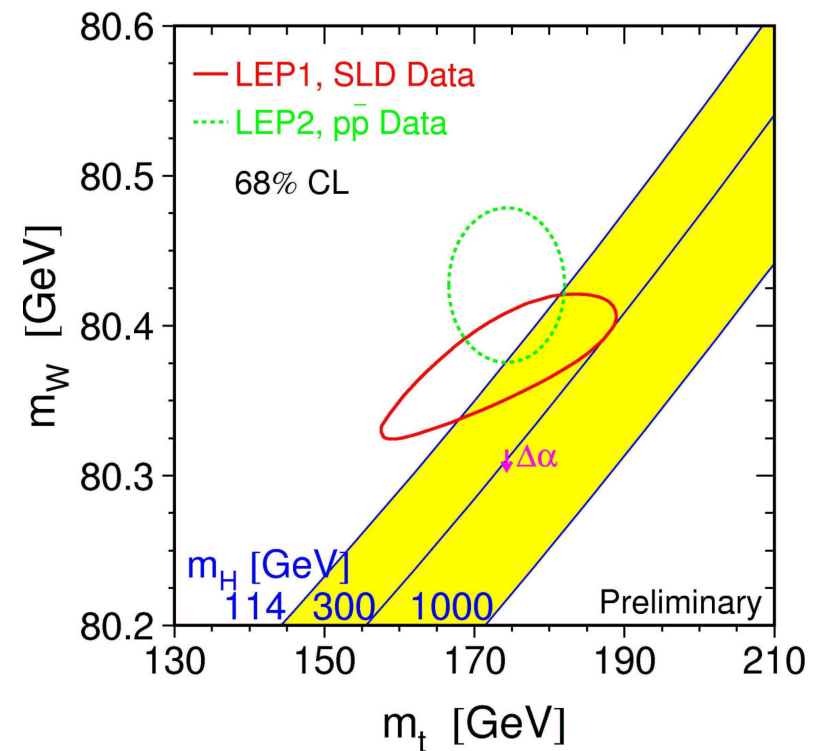
Precision EW measurements and the Higgs Boson



➤ Removing nuTeV has little effect on fit

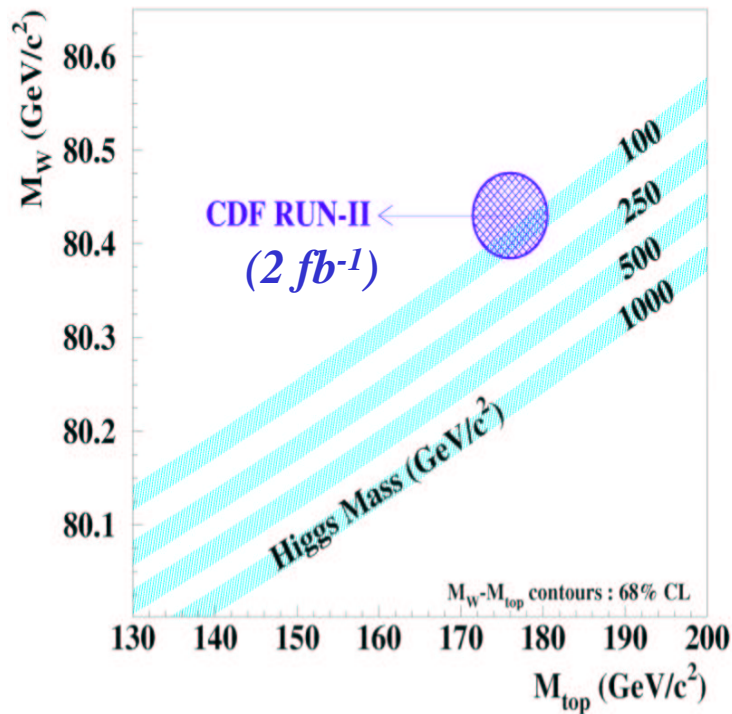
➤ Note: Poor quality of fit

$$M_h < 219 \text{ GeV}$$



Best fit: $M_h = 96^{+60}_{-38} \text{ GeV}$

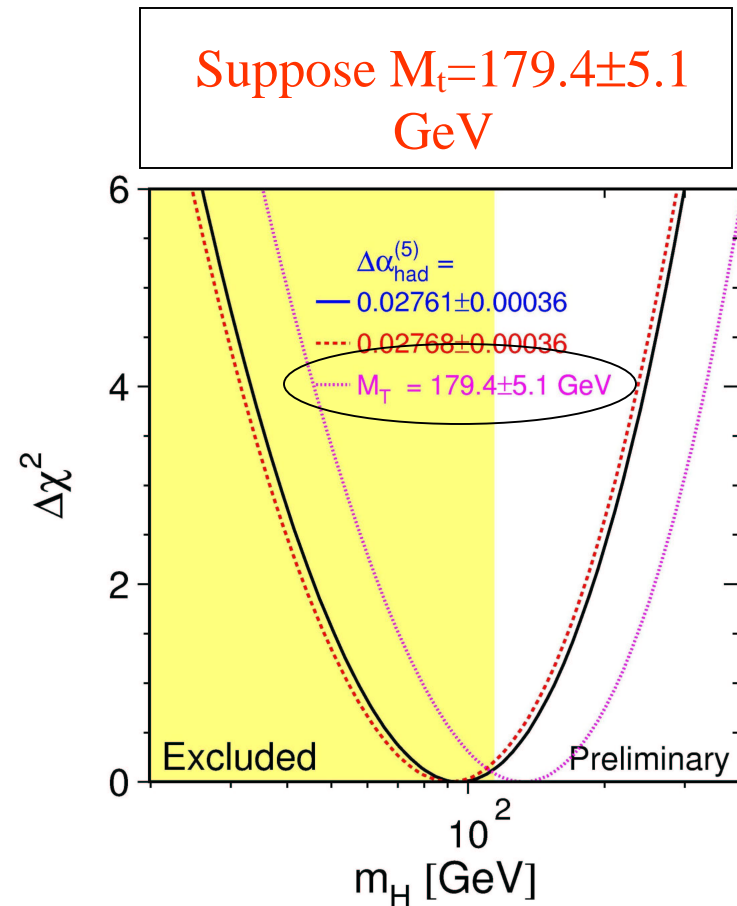
Top Mass has drastic Implications for M_h



M_h dependence is logarithmic

M_t dependence is quadratic

Increasing M_t by 5 GeV increases M_h limit by 35 GeV

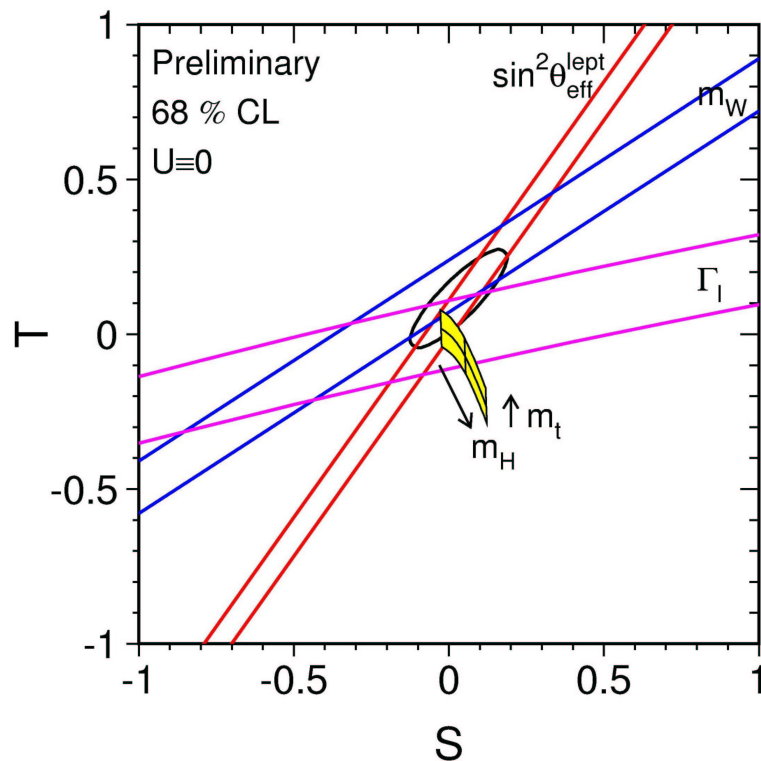


Limit on M_h goes from 219 GeV to $M_h < 283 \text{ GeV}$

Best fit goes from 96 GeV to 126 GeV

SM works well

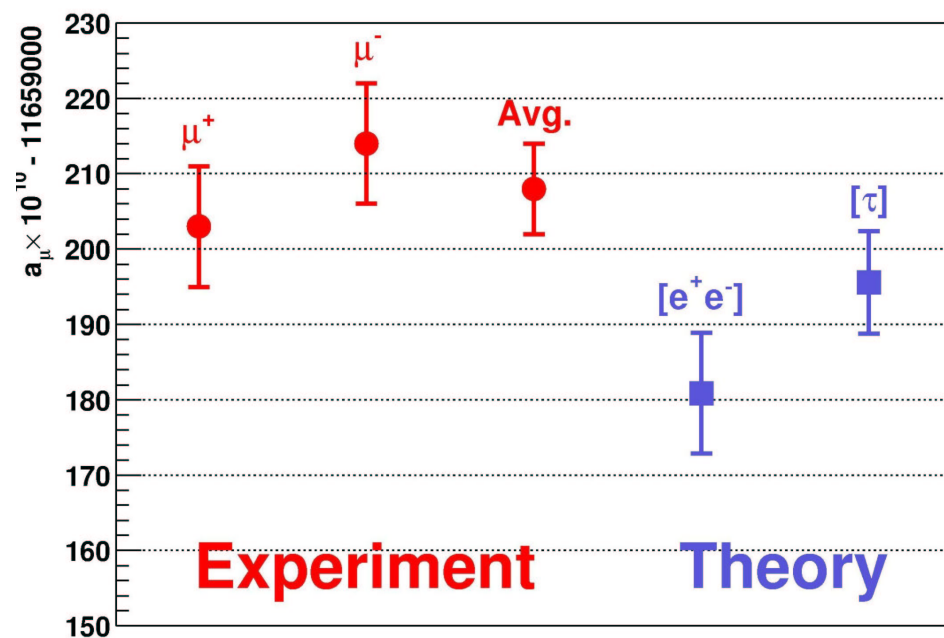
Fits to EW data



➤ Fit assumes $M_h = 150$ GeV

LEP EWWG 2003

New $(g-2)_\mu$ result

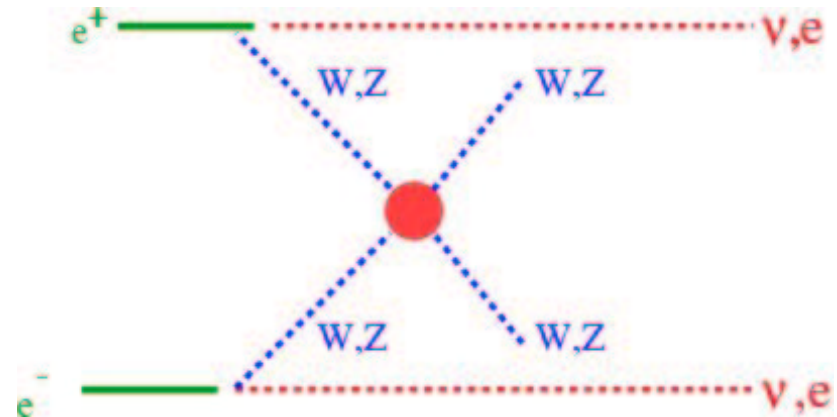
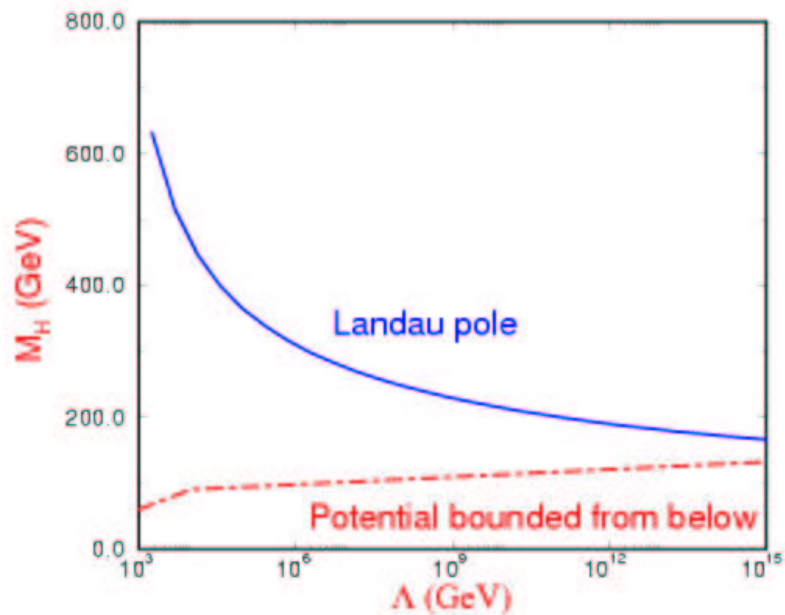


- e^+e^- data: 2.7σ effect
- τ data: 1.4σ effect

hep-ph/0401008

Where do we expect the Higgs?

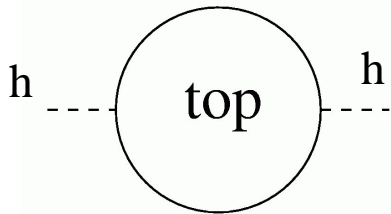
➤ Allowed Higgs mass region related to “Scale of New Physics”



➤ Standard Model inconsistent without Higgs unless new physics around 1.3 TeV

Light Scalars are unnatural

- Higgs mass grows with cut-off, Λ



$$\begin{aligned}\delta M_h^2 &= \frac{G_F}{4\sqrt{2}\pi^2} \Lambda^2 (6M_W^2 + 3M_Z^2 + M_h^2 - 12M_t^2) \\ &= -\left(\frac{\Lambda}{0.7 \text{ TeV}} 200 \text{ GeV} \right)^2\end{aligned}$$

$M_h \leq 200 \text{ GeV}$ requires large cancellations

The SM as an Effective Theory

- The SM is an effective low energy theory
 - Valid below some scale Λ
 - Assumes no new EW scale particles
- New physics effects parameterized in terms of higher dimension operators with SM fields
- 2 possibilities:
 - No Higgs \Rightarrow Non-linear realization
 - Light Higgs \Rightarrow Effective operators with Higgs bosons
- Assume CP, baryon #, lepton #, conservation

Assume light Higgs

- Effects of new physics appears as dimension 6 operators constructed with low energy fields

$$L_{eff} = L_{SM} + \sum \frac{f_i}{\Lambda^2} O_i + \dots$$

- 12 CP conserving operators in Higgs/gauge sector
- Consider operators which affect W,Z 2-pt functions

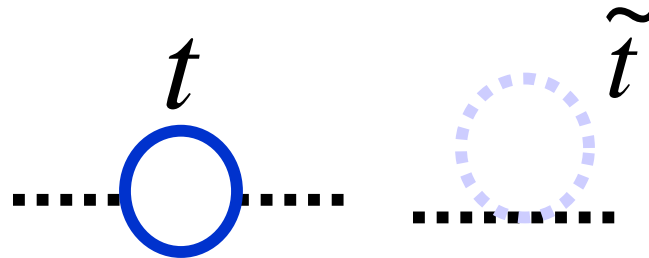
$$O_{BW} = -\frac{gg'}{2} \varphi^+ B_{\mu\nu} W^{\mu\nu} \varphi$$
$$O_{\varphi,1} = (D_\mu \varphi)^+ \varphi^+ (D^\mu \varphi)$$

- LEP: $O_{\varphi,1} \Rightarrow \Lambda > 5 \text{ TeV}$

Little Hierarchy: What explains why $\Lambda > 1 \text{ TeV}$?

SUSY....Our favorite model*

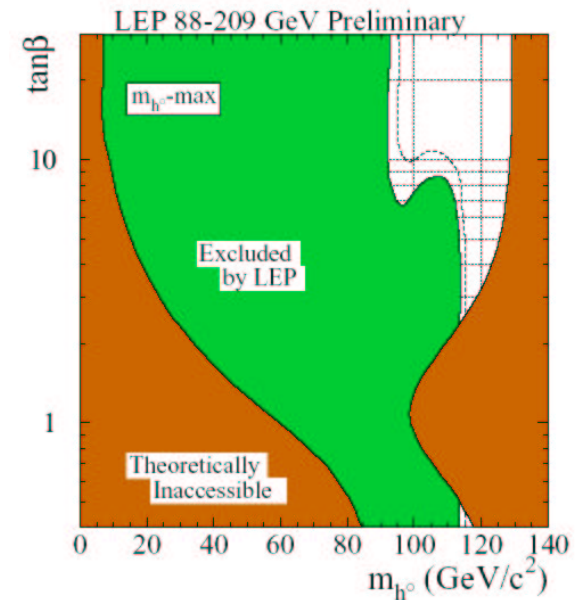
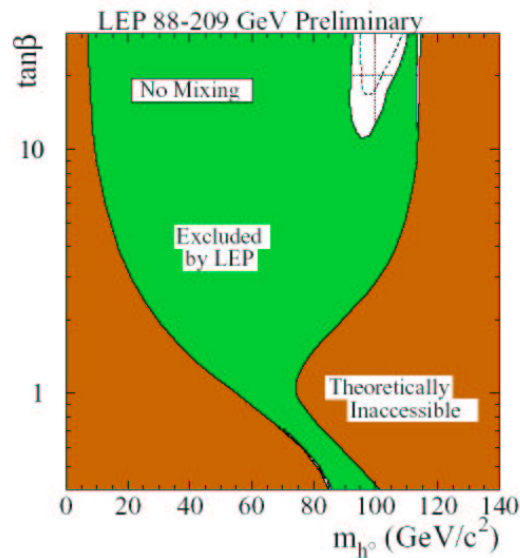
- Quadratic divergences cancelled automatically if SUSY particles at TeV scale
- Cancellation result of *supersymmetry*, so happens at every order



$$\delta M_h^2 \approx (\dots) G_F \Lambda^2 (M_t^2 - M_{\tilde{t}}^2)$$

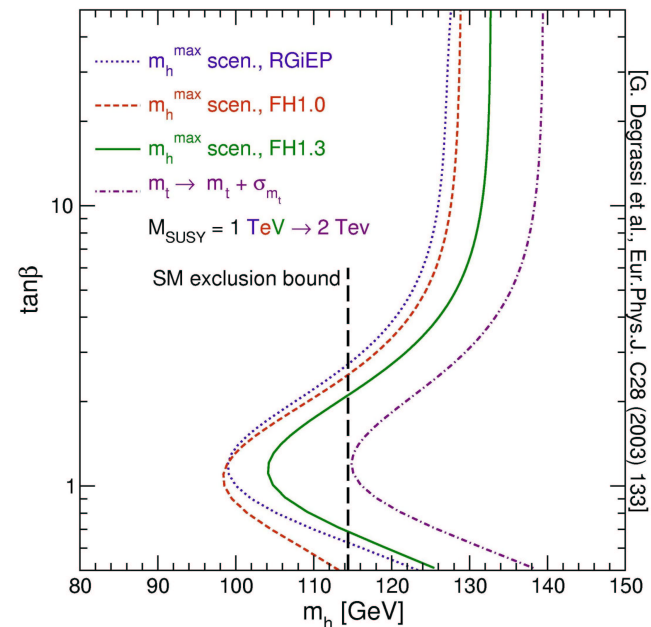
* Spires: 7421 papers after 1990 with title supersymmetry or supersymmetric!

LEP MSSM Higgs Bound



- Boundaries of theoretically inaccessible region ("the nose") have shifted due to 2-loop calculations of MSSM Higgs mass

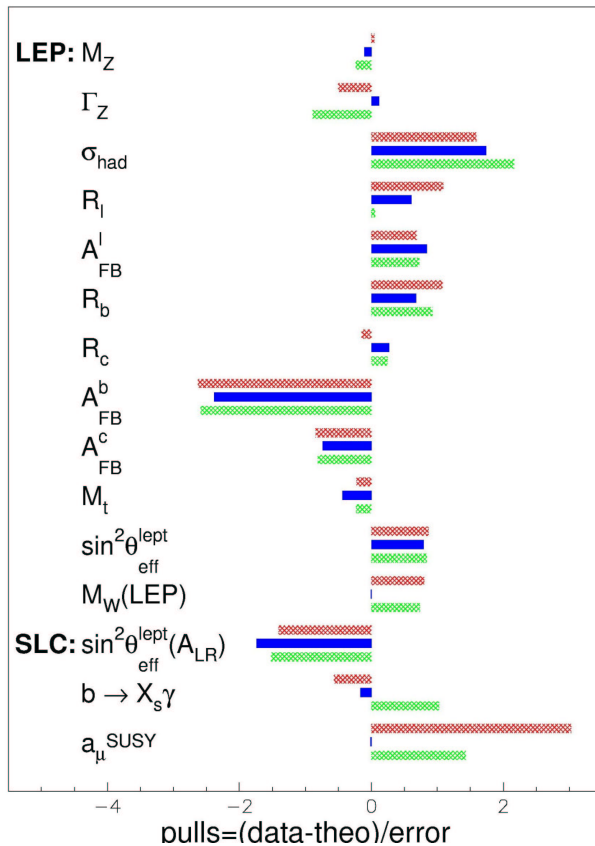
With $m_t=179 \text{ GeV}$, $\tan\beta$ exclusion disappears!



Precision measurements consistent with MSSM

- Fit precision data to MSSM

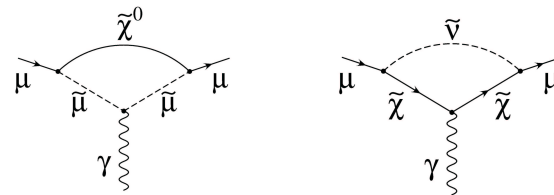
SM: $\chi^2/\text{d.o.f} = 27.2/16$
 MSSM: $\chi^2/\text{d.o.f} = 16.4/12$
 CMSSM: $\chi^2/\text{d.o.f} = 23.2/16$



MSSM slightly better fit (17% prob)
vs SM (5% prob)

MSSM prefers “light” SUSY

$(g-2)_\mu$ and $b \rightarrow s \gamma$ can be made to agree better with predictions by including light SUSY



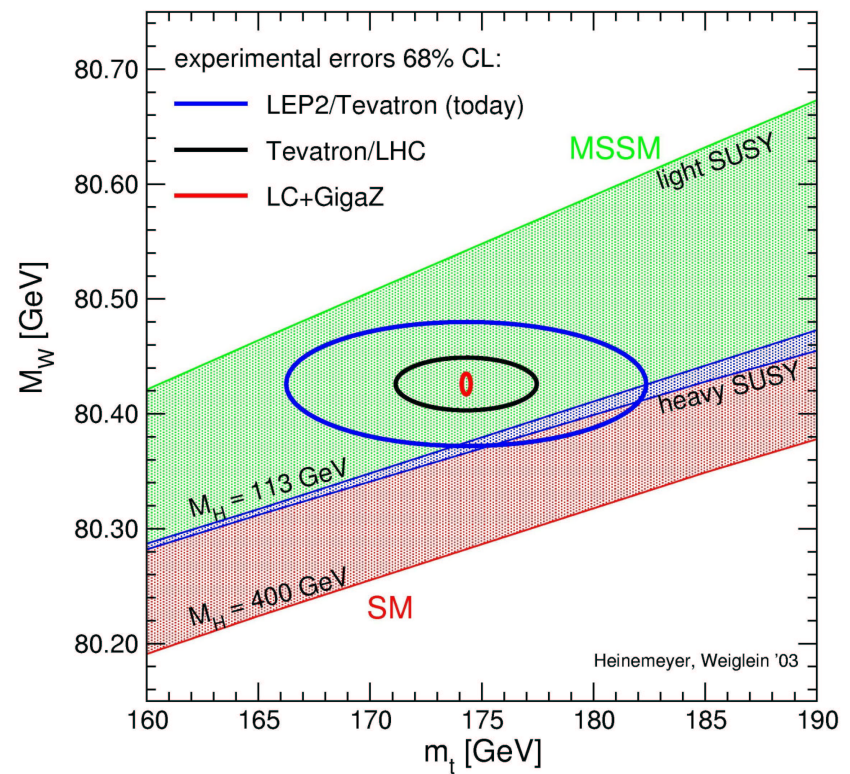
CMSSM: 5 parameters

$m_0, m_{1/2}, A_0 \tan\beta, \text{sign } \mu$

➤ Fit not as good as MSSM

Motivation for light SUSY....

- Improves SM fit
- Has Higgs boson just around the corner
- Large discovery potential at LHC/LC

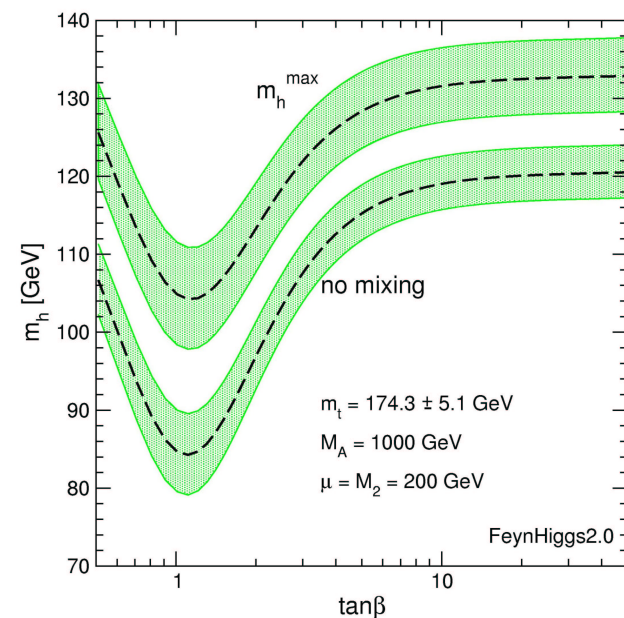


MSSM requires light Higgs

- **Tension:** stop should be **TeV scale** to cancel quadratic divergences in M_h from top loops
- Stop needs to be **heavy** so that lightest Higgs mass satisfies LEP bound,

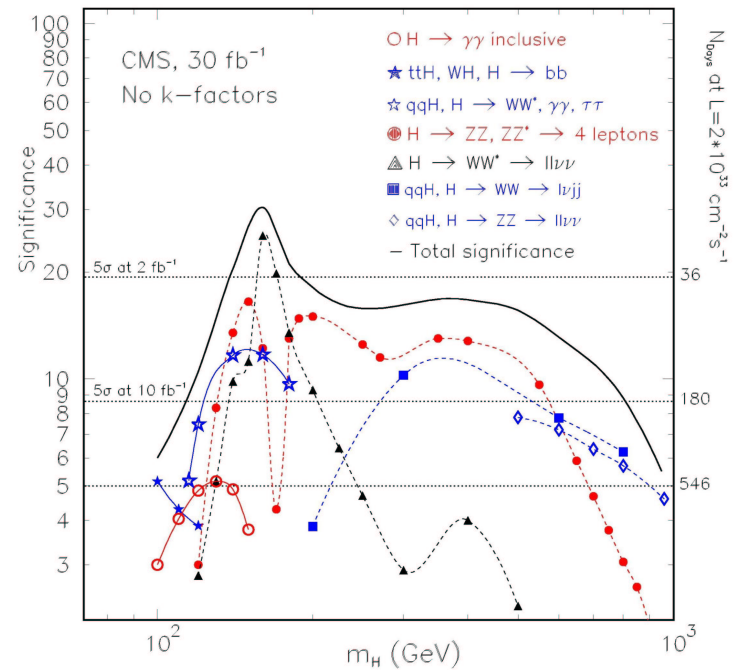
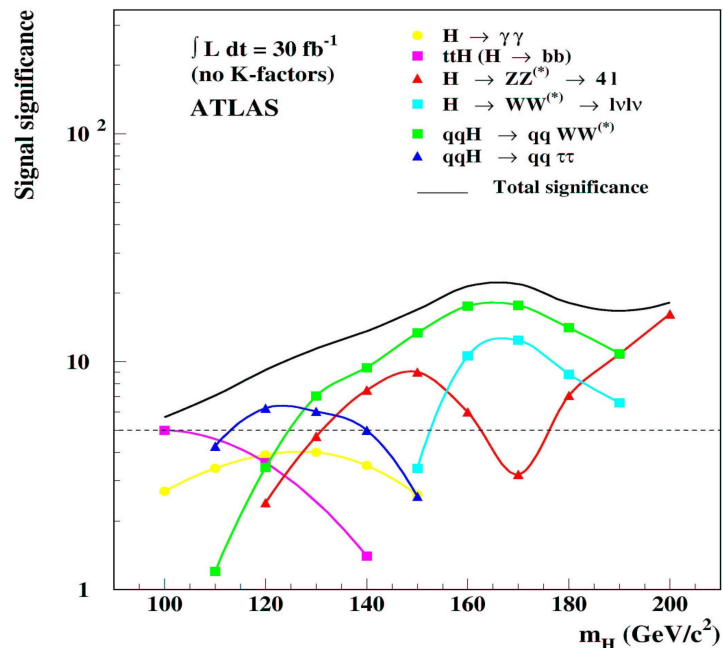
$$M_h > 114 \text{ GeV}$$

$$M_h^2 \leq M_Z^2 \cos^2 2\beta + \frac{3G_F m_t^4}{\sqrt{2}\pi^2 \sin^2 \beta} \ln \left[\frac{\tilde{m}_t^2}{m_t^2} \right] + \dots$$



Degrassi, Heinemeyer, Holliuk, Slavich,
Weiglein, hep-ph/0212020

If there is a light SM Higgs, we'll
find it at the LHC



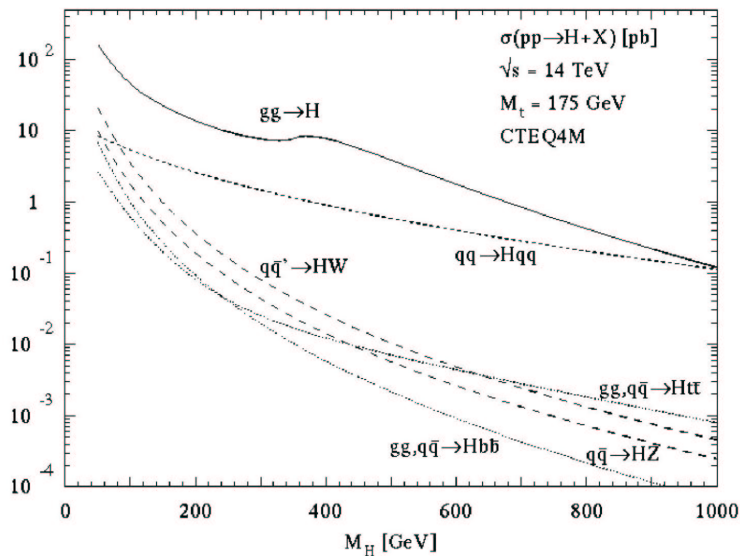
No holes in M_h coverage

Discovery happens early in the game!

(plots are 30 fb^{-1})

Higgs at the LHC

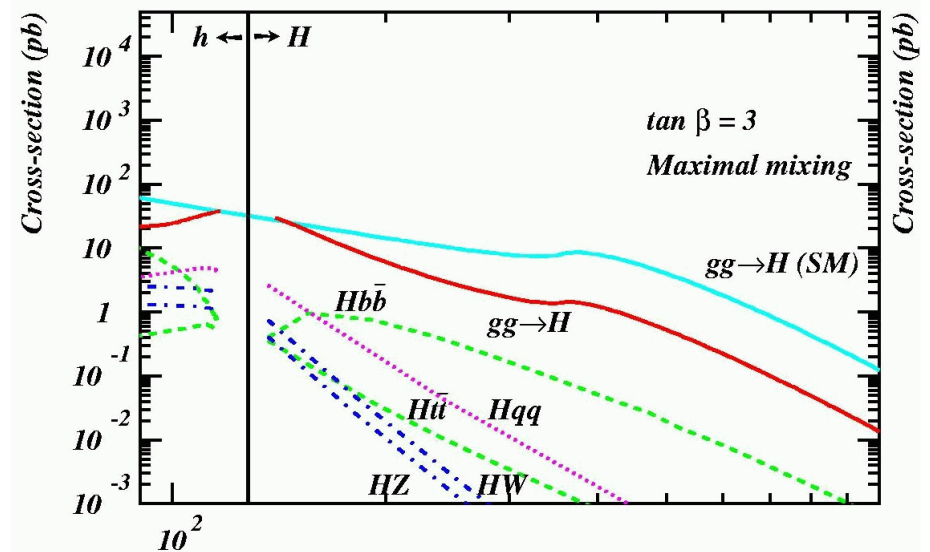
SM:



➤ In SM $\sigma(bbh) \ll \sigma(gg \rightarrow h)$

For $M_h < 250$ GeV, $\sigma(bbh) > \sigma(tth)$

SUSY:



➤ For small $\tan \beta$, $\sigma(bbh)$ highly suppressed

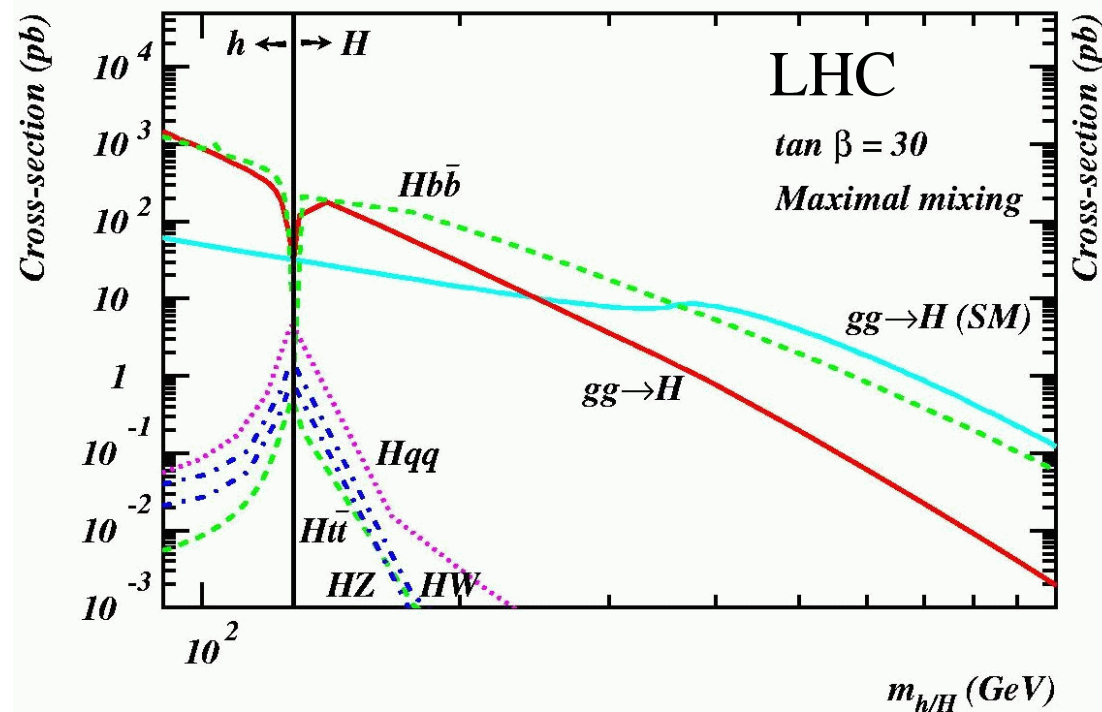
b's add new wrinkle to Higgs production in SUSY

- Couplings of b to H/A enhanced at large $\tan \beta$
- $bb \rightarrow H/A$ can dominate because:

$$\sigma_{bb} \approx \frac{m_b^2}{M_h^2} \tan^2 \beta$$
$$\sigma_{gg} \approx C_1 \cot^2 \beta + C_2 \frac{m_b^2}{M_h^2} + C_3 \frac{m_b^4}{M_h^4} \tan^4 \beta$$

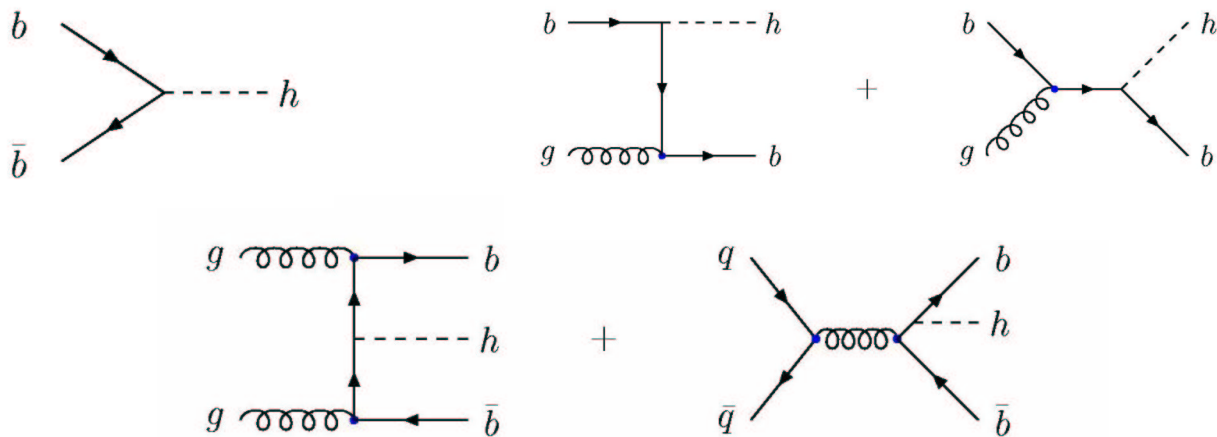
Production of SUSY Higgs Bosons

- For large $\tan \beta$, dominant production mechanism is with b's
- bbh can be 10x's SM Higgs rate in SUSY for large $\tan \beta$



What is the dominant process?

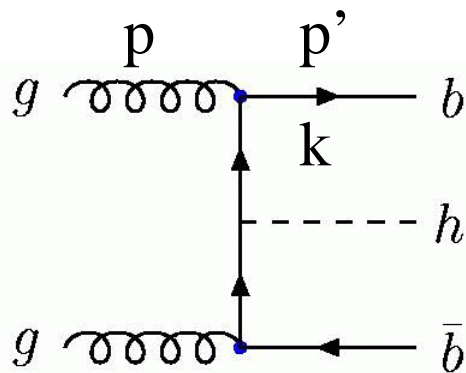
$$pp \rightarrow b\bar{b}h$$



*Answer depends on whether
you tag outgoing b 's*

Collinear Singularities

- $g \rightarrow bb$ splitting
 - Singular when b 's are collinear with initial gluon
 - m_b regulates singularity



Collinear limit:

$$p' = (1-z)p$$

$$k = zp$$

Internal propagator:

$$\frac{1}{(k^2 - m_b^2)} \rightarrow -\frac{1}{m_b^2}$$

$$|A(gg \rightarrow b\bar{b}h)|^2 \rightarrow (4\pi\alpha_s) |A(bg \rightarrow b\bar{b}h)|^2 \frac{P_{gb}(z)}{p \cdot p'}$$

The b quark as a parton

Phase space also factorizes in collinear limit:

$$(PS)_3 \rightarrow (PS)_2 (\cdots) \int \frac{dE_b}{E_b}$$

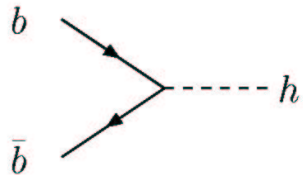
- Integration over b phase space gives large log
- Absorb log into b quark distribution

$$b(x, \mu) = \frac{\alpha_s}{2\pi} \ln\left(\frac{\mu^2}{Q^2}\right) \int_x^1 \frac{dz}{z} P_{bg}\left(\frac{x}{z}\right) g(z, \mu)$$

- Altarelli-Parisi evolution of PDFs sums $\alpha_s^n \ln^n(Q^2/m_b^2)$
 - Initial condition, $b(x, m_b) = 0$
- b quark PDF $\approx \alpha_s \ln(Q^2/m_b^2)$ relative to gluon PDF
- Construct algorithm for including b's as initial state partons

Consistent Counting for b initiated processes

Large logarithms summed into b quark PDFs



$$(\alpha_s \ln(M_h^2/m_b^2))^2$$



$$\alpha_s^2 \ln(M_h^2/m_b^2)$$

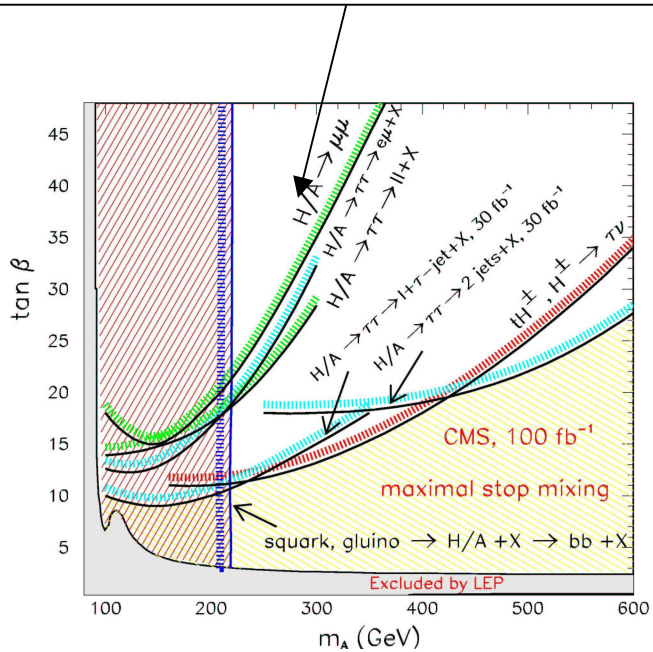


$$\alpha_s^2$$

Dicus & Willenbrock, PRD39, 751 (1989)

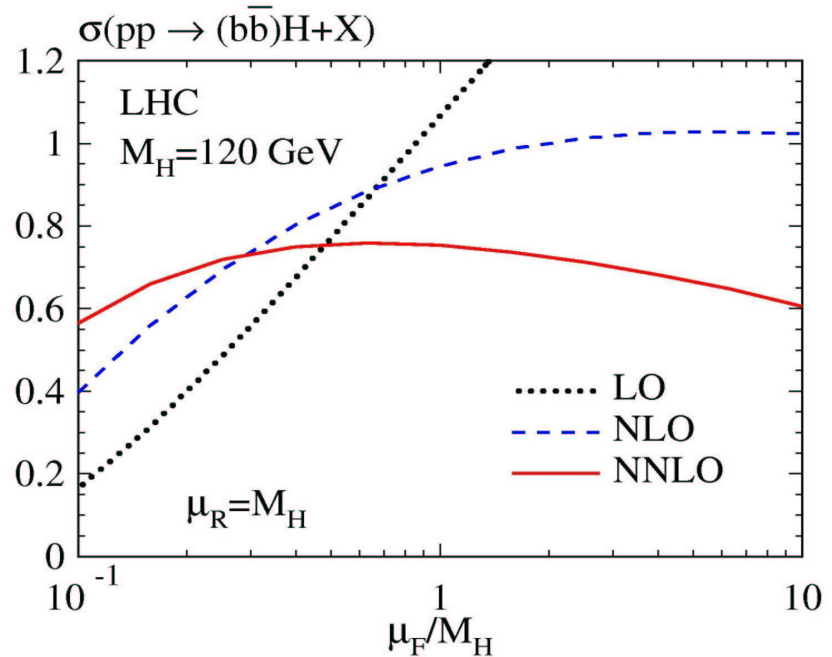
bb→h in MSSM

Single Higgs observable at large $\tan \beta$ through $H/A \rightarrow \mu^+ \mu^-, \tau^+ \tau^-$



➤ Single Higgs rate computed from $gg \rightarrow h$ in CMS plot

Reduced theoretical error
from reduced μ dependence



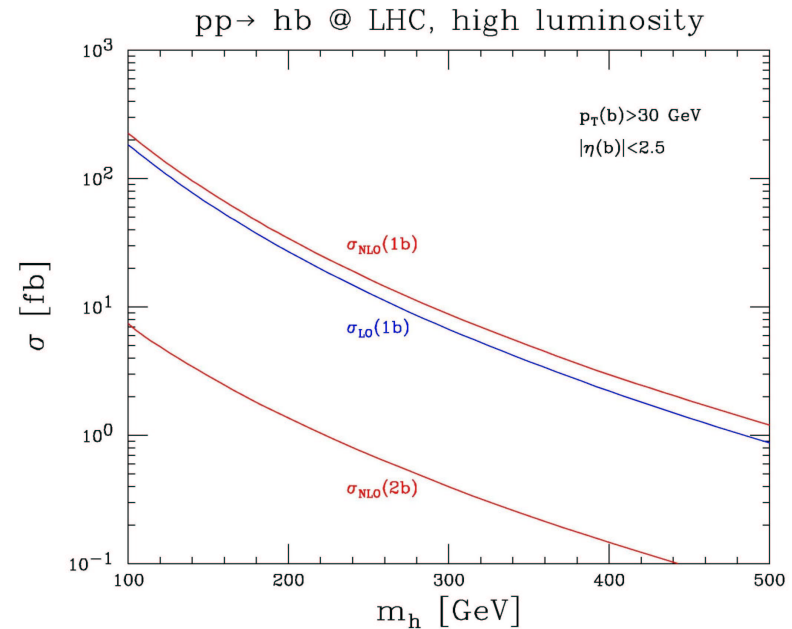
NLO: Maltoni, Sullivan, & Willenbrock, hep-ph/0301033

NNLO: Harlander & Kilgore, hep-ph/0304035

bh production at NLO

- More promising channel than $bb \rightarrow h$
- Extra b tag and Higgs transverse momentum improve detection efficiency

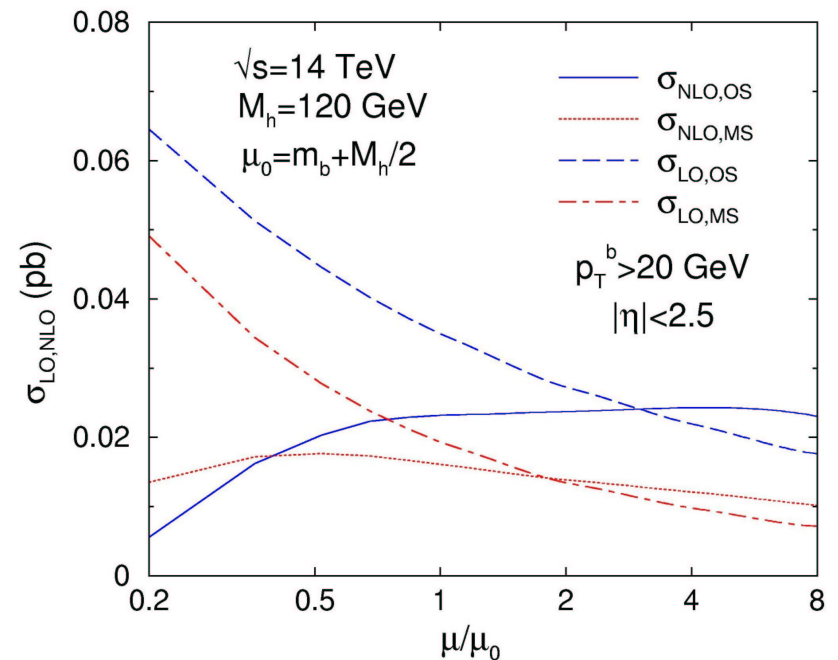
SM at LHC:



gg→bbh at NLO

- Rate proportional to b quark Yukawa Coupling, m_b/v
- Lore: \overline{MS} b mass sums logarithms

$$\overline{m}_b(\mu) = m_b \left(1 - \frac{\alpha_s(\mu)}{4\pi} \left[3 \ln \left(\frac{\mu^2}{m_b^2} \right) + 4 \right] \right)$$
- Clearly true for $h \rightarrow b\bar{b}$
- Many sources of logs in production process
- Large residual scheme dependence at NLO: formally $O(\alpha_s^4)$

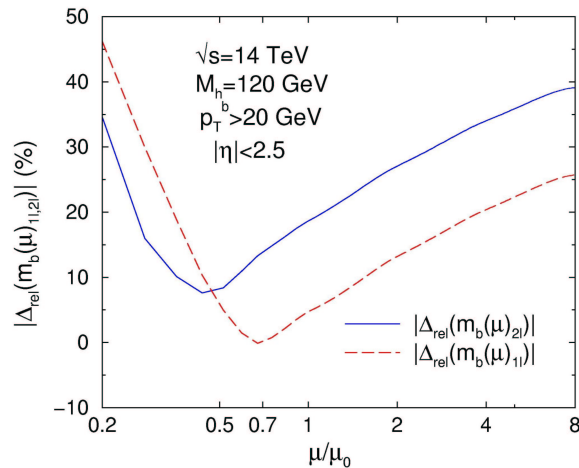


Dawson, Jackson, Reina, Wackerth, hep-ph/0311067

Dittmaier, Kramer, Spira, hep-ph/0309204

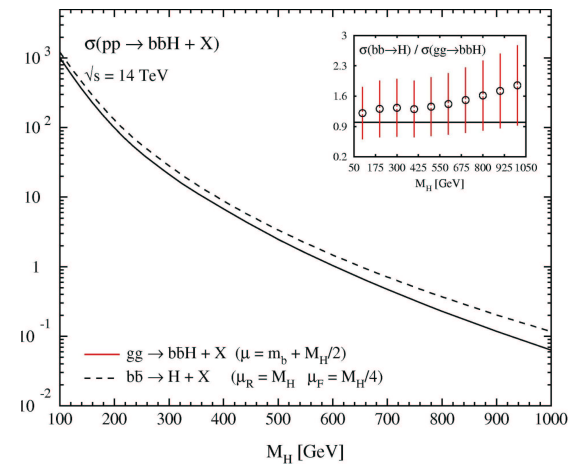
Theoretical Issues

- Large remaining scale/scheme dependence between OS and \overline{MS} at NLO



- Effect ≈ 10 -20%

$gg \rightarrow b\bar{b}h$ vs $b\bar{b} \rightarrow h$ at NLO



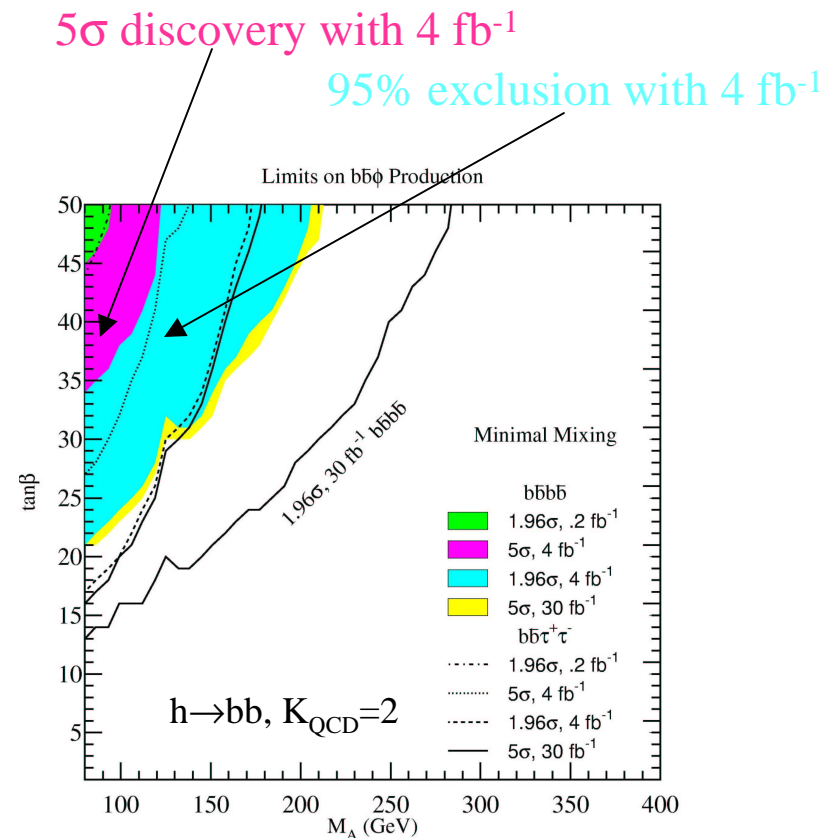
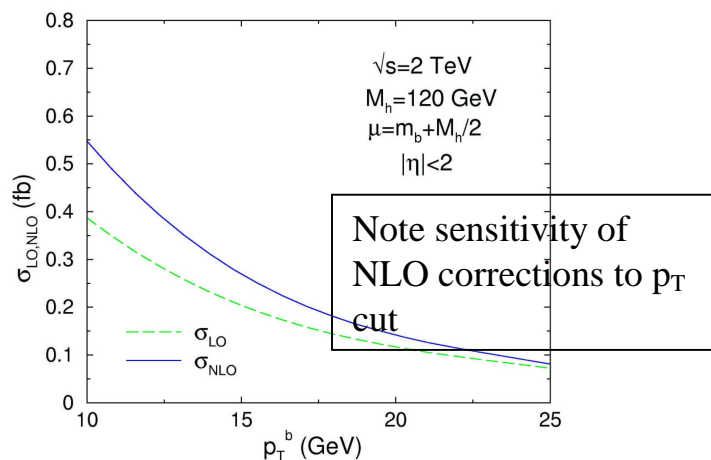
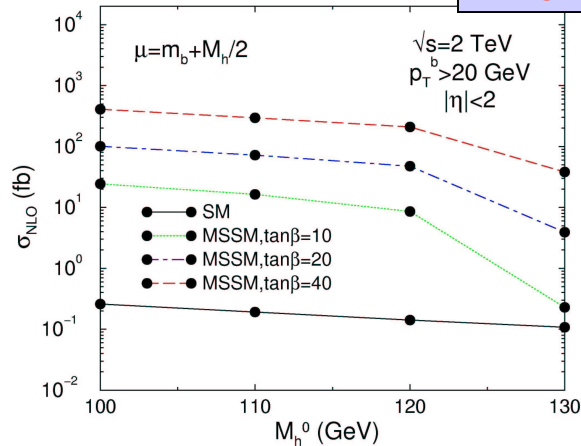
Note scale choice, $\mu=M_h/4$

Dittmaier, Kramer, Spira, Les Houches03

Maltoni, Sullivan, Willenbrock, hep-ph/0301033

bbh in SUSY Models at Tevatron

Huge enhancements in SUSY

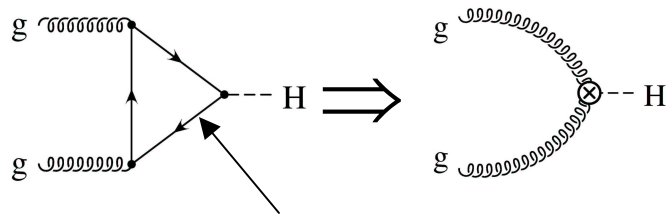


Dawson, Jackson, Reina, Wackerroth, hep-ph/0311067

Carena, Mrenna, Wagner, hep-ph/9808312

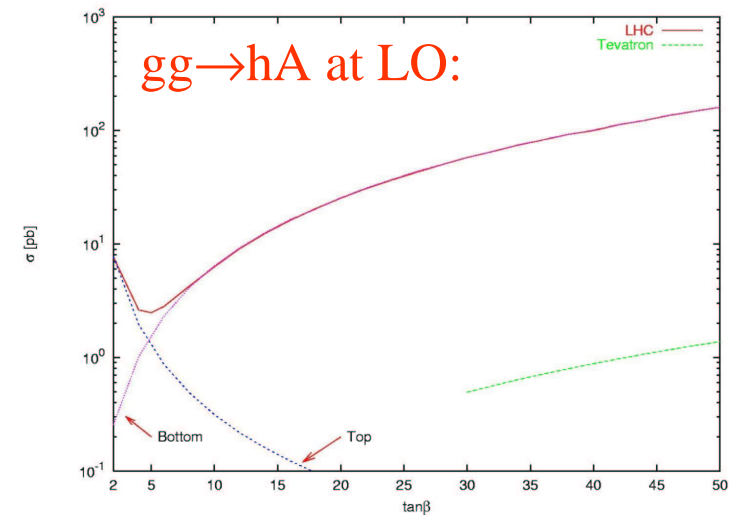
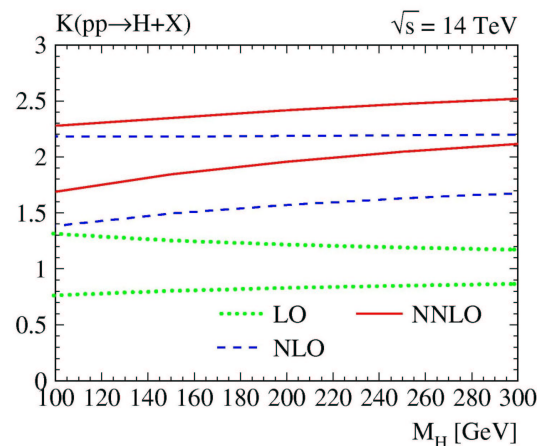
Dittmaier, Kramer, Spira, hep-ph/0309204

NNLO corrections done in large m_t effective theory



Only top in loop

- Effective theory not valid when b contributions important



- $\tan \beta > 5$, b loops dominate

Harlander & Kilgore, hep-ph/0201206,

Anastasiou, Melnikov, hep

Field, Dawson, Smith, hep-ph/0311199

One Argument for MSSM is Grand Unification

- 1 loop RGE, SU(5) normalization of U(1):

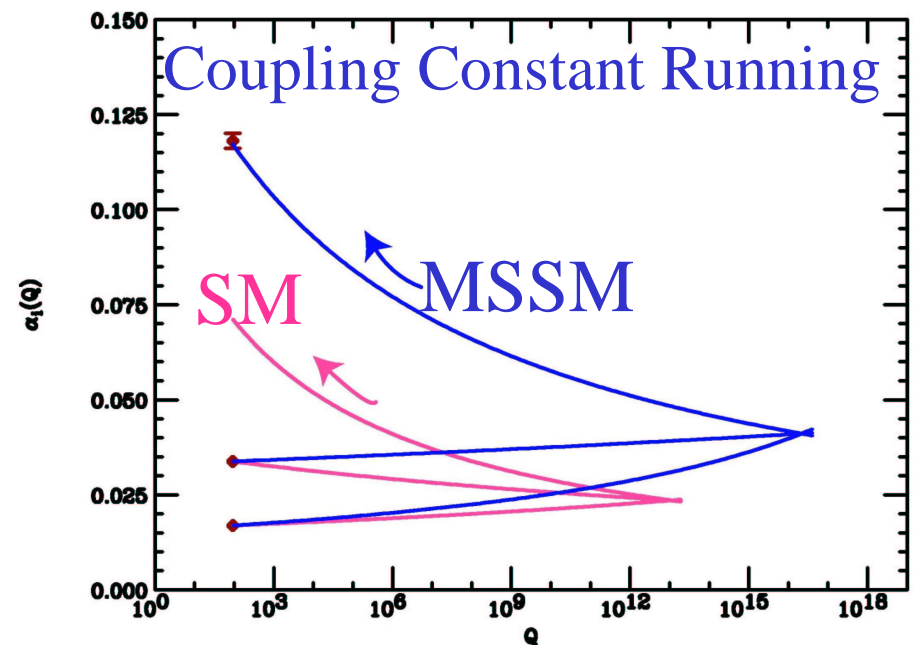
$$B = \frac{1/\alpha_3 - 1/\alpha_2}{1/\alpha_2 - 1/\alpha_1} = .53(SM), .71(MSSM)$$

- Experimentally, $B = .717 \pm .008$
- 2 loop RGE, TeV scale threshold effects weaken argument:

$$\text{MSSM: } \alpha_s(M_Z) > .13$$

$$\text{PDG: } \alpha_s(M_Z) = .1171 \pm .0014$$

- Restoring agreement requires large GUT scale corrections



Peskin, hep-ph/0212204

Gauge Singlets don't spoil Unification

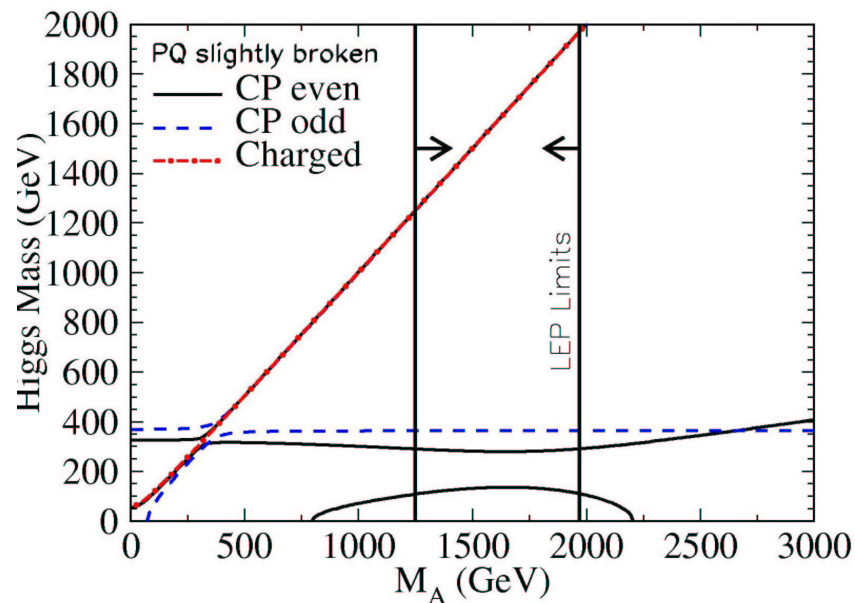
- Simplest modification of MSSM: add Higgs singlet S
- Superpotential, $W = \lambda_1 H_u H_d S + \frac{\kappa}{3} S^3$
 - S^3 term necessary to avoid PQ Axion
 - $\lambda \langle S \rangle H_u H_d$ naturally generates $\mu H_u H_d$ term
- At tree level, lightest Higgs mass bound becomes,

$$M_h^2 \leq M_Z^2 \cos^2 2\beta + v^2 \lambda_1^2 \sin^2 2\beta$$

- Assume couplings perturbative to M_{GUT} and SUSY scale ≈ 1 TeV
 - $M_h < 150$ GeV with singlet Higgs
- Singlets can be consistent with precision measurements
- Phenomenology very different from MSSM
 - 3 neutral Higgs boson, 2 pseudoscalars, 1 charged Higgs
 - Many scenarios have h, A at weak scale

NMSSM Higgs Mass Spectrum

Typical Scenario:

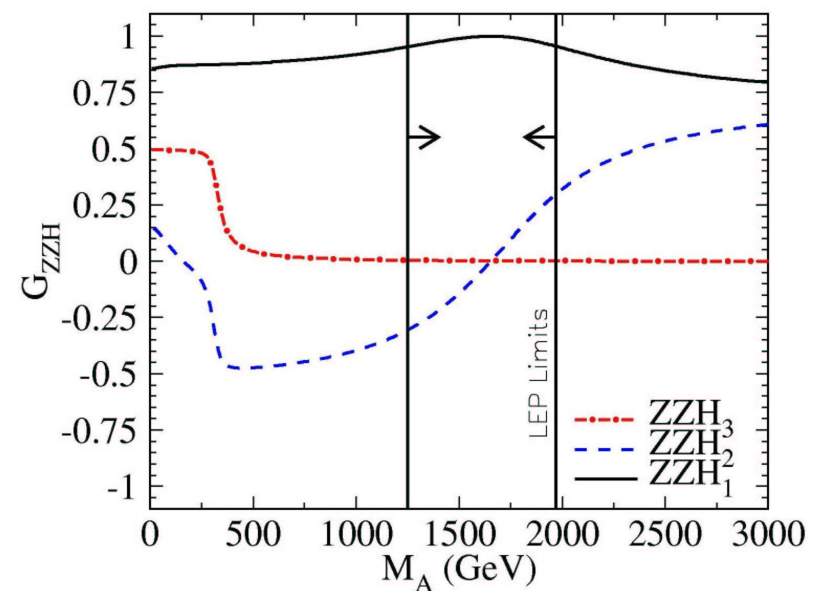


➤ Heavy, roughly degenerate H_3, A_2, H^\pm

➤ Spectrum of light Higgs: 2 light scalars, 1 light pseudoscalar

Very different from MSSM!

ZHH couplings suppressed



New Decays:

$A_1 \rightarrow H_1 H_1, H_2 \rightarrow A_1 A_1$

Miller, Nevzorov, Zerwas, hep-ph/0304049

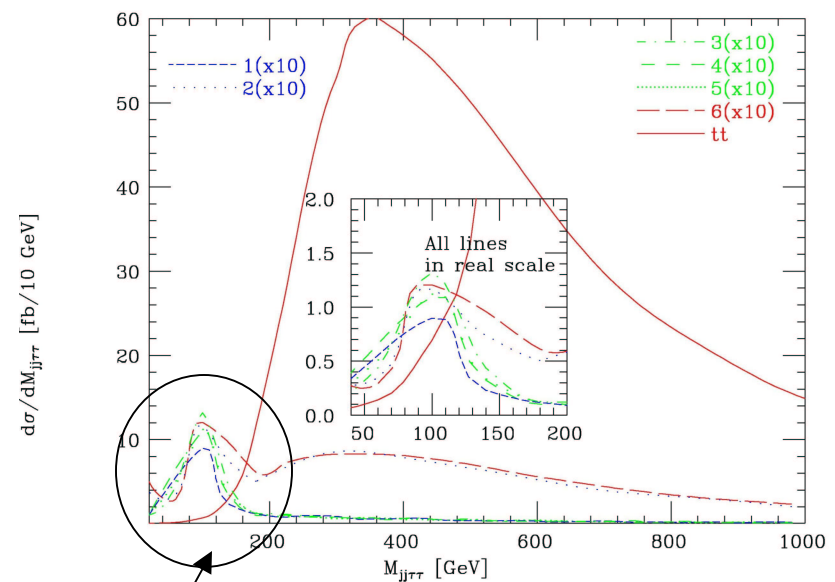
MSSM, $h \rightarrow AA$ excluded Experimentally

- $h \rightarrow AA$ important discovery channel in NMSSM
- h can be SM-like and A light in NMSSM
- Look for
 - $W^+W^- \rightarrow h \rightarrow AA \rightarrow \tau^+\tau^- jj$
 - Dominant background from tt
 - Statistically significant at LHC with $300 \text{ fb}^{-1}/\text{detector}$

• Look for enhancement at low mass

• Not Gold-Plated!

Curves are different models

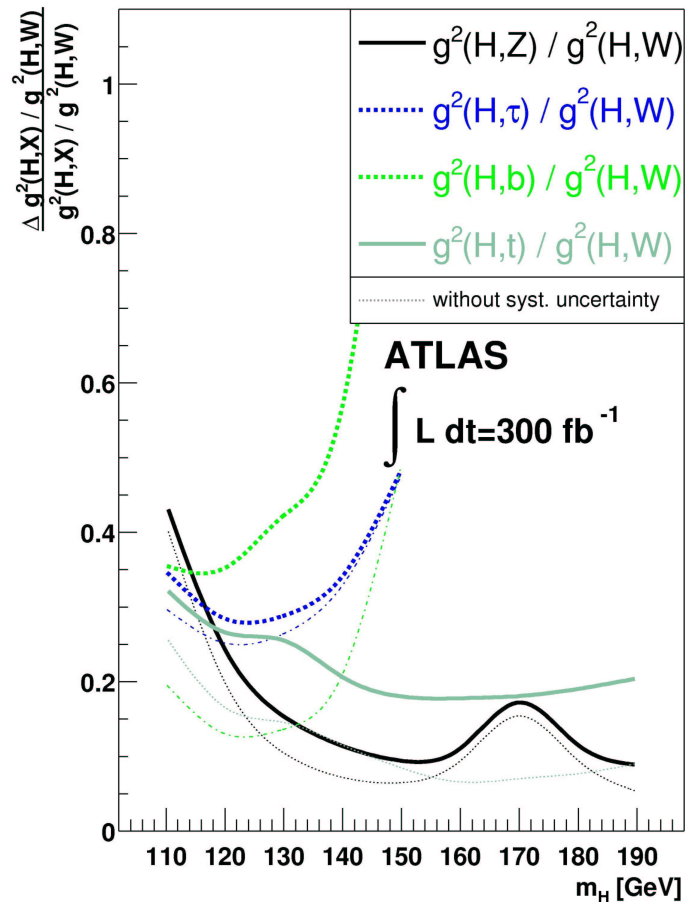


Ellwanger, Gunion, Hugonie,
Moretti, hep-ph/0305109

If we find a “Higgs-like” object, what then?

- We need to:
 - Measure Higgs couplings to fermions & gauge bosons
 - Measure Higgs spin/parity
 - Reconstruct Higgs potential
- Reminder: Many models have other signatures:
 - New gauge bosons (little Higgs)
 - Other new resonances (Extra D)
 - Scalar triplets (little Higgs, NMSSM)
 - Colored scalars (MSSM)
 - etc

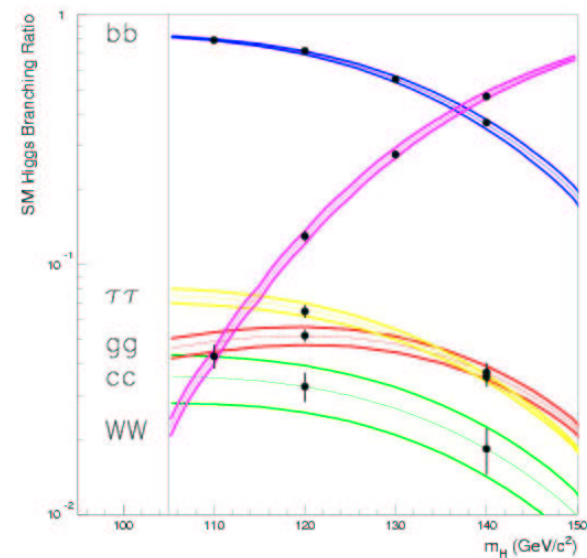
Absolute measurements of Higgs couplings



Duhrssen, ATL-PHYS-2003-030

e^+e^- LC at $\sqrt{s}=350 \text{ GeV}$

$L=500 \text{ fb}^{-1}$, $M_H=120 \text{ GeV}$



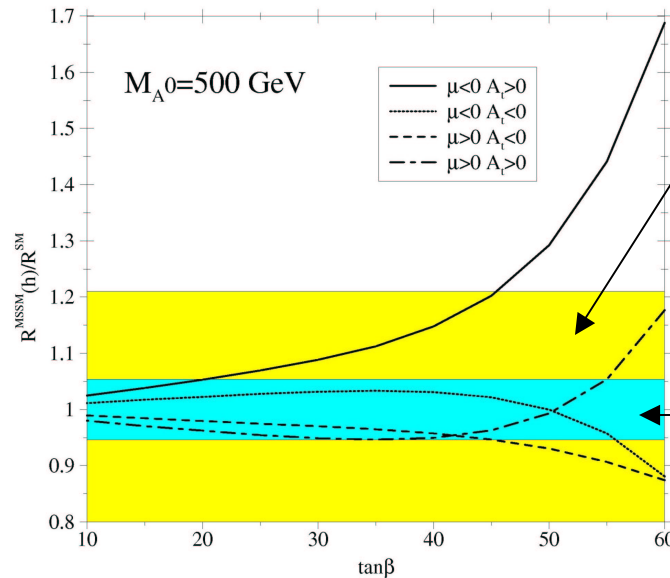
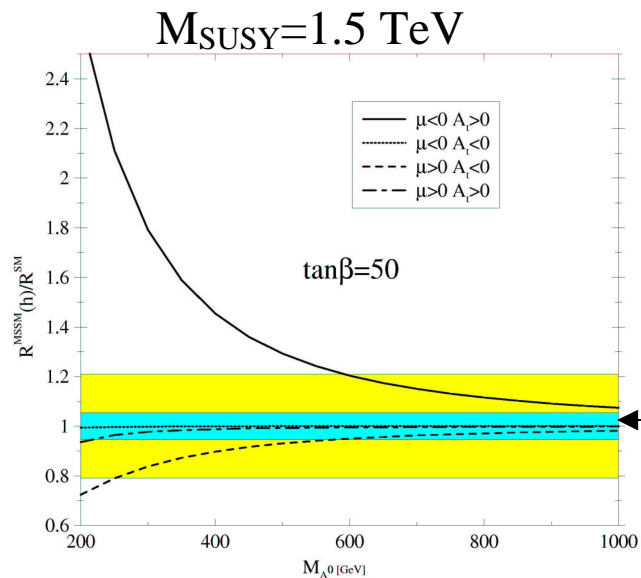
Battaglia, Desch, hep-ph/0101165

LC can measure g_{ZZh} to 1-2%
 through $\sigma(e^+e^- \rightarrow Zh)$

How well do we need Higgs couplings?

- MSSM example:

$$R = \frac{BR(h \rightarrow b\bar{b})}{BR(h \rightarrow \tau^+\tau^-)}$$



21% deviation
from SM

5.4% deviation
from SM

Note rapid approach to
decoupling limit

Conclusions

- SM works well with light Higgs
 - Scale for extensions pushed by precision measurements
- Role of b quark in Higgs production calculations in MSSM presents new theoretical challenges
 - New production mechanisms
 - Need for NNLO without large m_t effective theory
- We need to think outside the MSSM box
 - New effects in NMSSM
 - Precision measurements of Higgs couplings can distinguish between models